



復旦大學

Fudan University



# Testing black holes using X-ray reflection spectroscopy

**Cosimo Bambi**

**Fudan University**

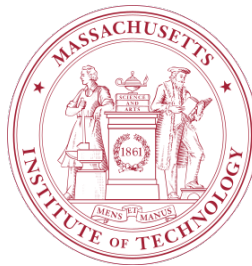
<http://www.physics.fudan.edu.cn/tps/people/bambi/>



**HEP Remote Video Seminar Series @ IIT Hyderabad, 4 October 2018**

## Contributors

**Askar Abdikamalov, Dmitry Ayzenberg, Zheng Cao,  
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Ashutosh Tripathi, Jack Steiner, Jingy Wang, Yerong Xu**



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TÜBINGEN



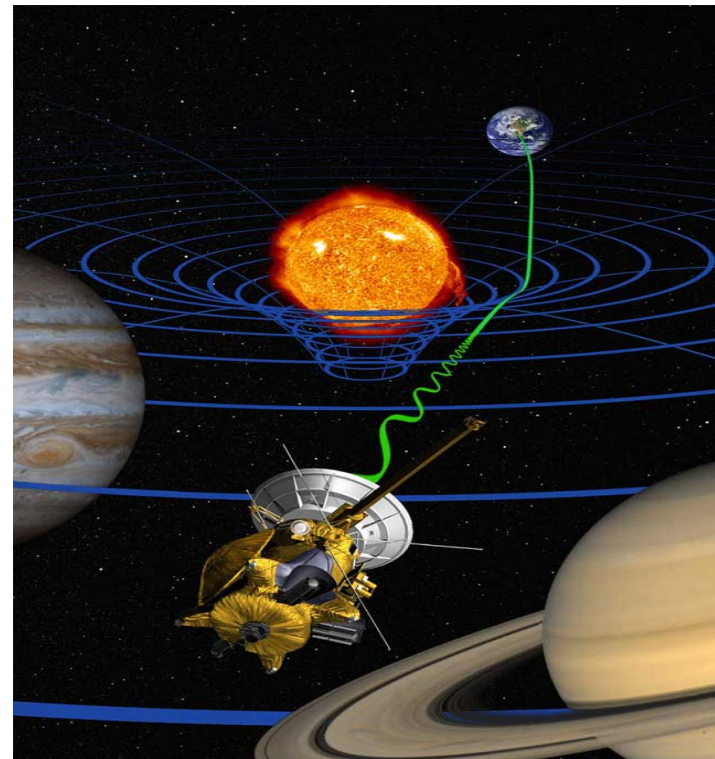
# **Motivations**

# Tests of general relativity

- **1915 → General relativity (Einstein)**
- **1919 → Deflection of light by the Sun (Eddington)**
- **1960s-present → Solar System experiments**
- **1970s-present → Binary pulsars**

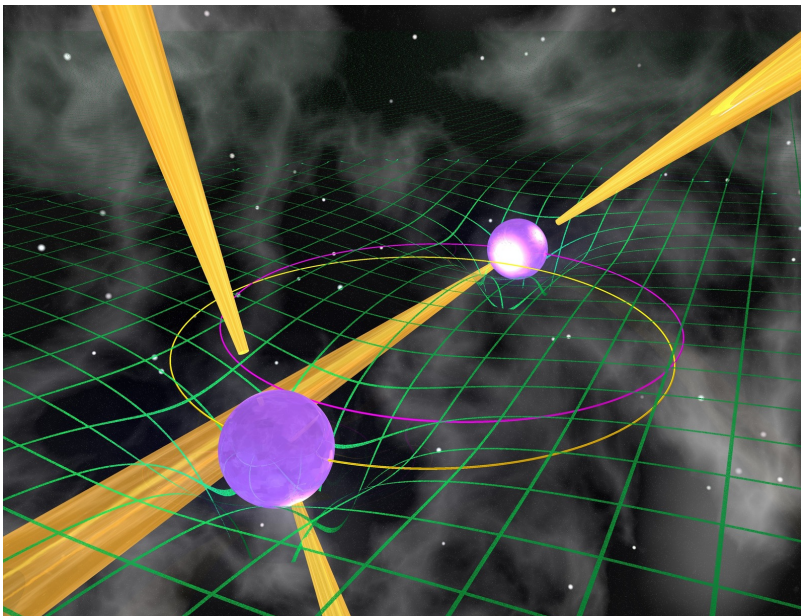
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- 1915 → General relativity (Einstein)
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- **Weak fields**
- **Today → Black holes**



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- **1960s-present → Solar System experiments**

- **1970s-present → Binary pulsars**

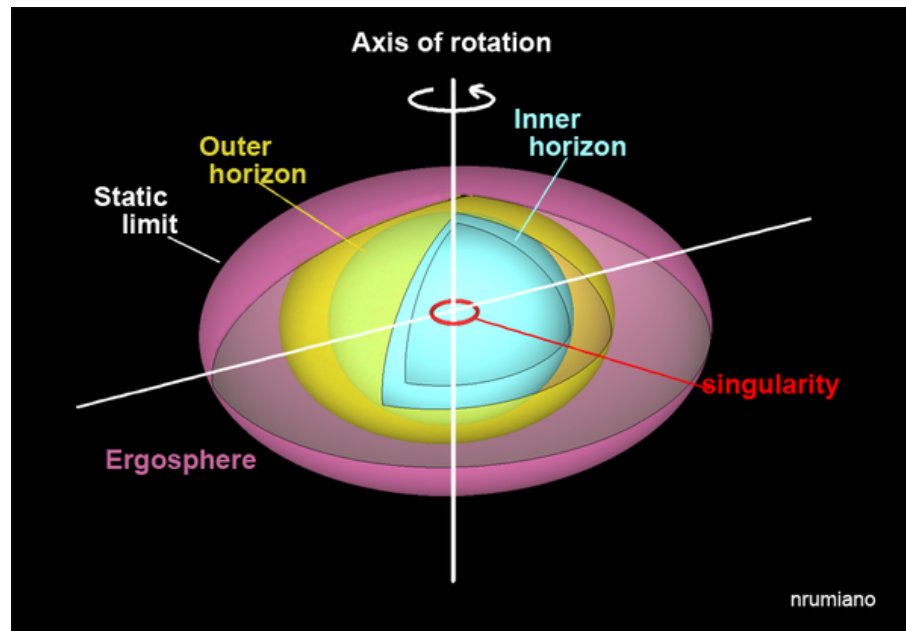
→ **Weak fields**

- **Today → Black holes**

→ **Strong fields**

# Black holes in Einstein's Gravity

- “No-Hair Theorem”  $\rightarrow M, J, Q$  ( $a_* = J/M^2$ )
- Uncharged black holes  $\rightarrow$  Kerr solution
- Clear predictions on the particle motion



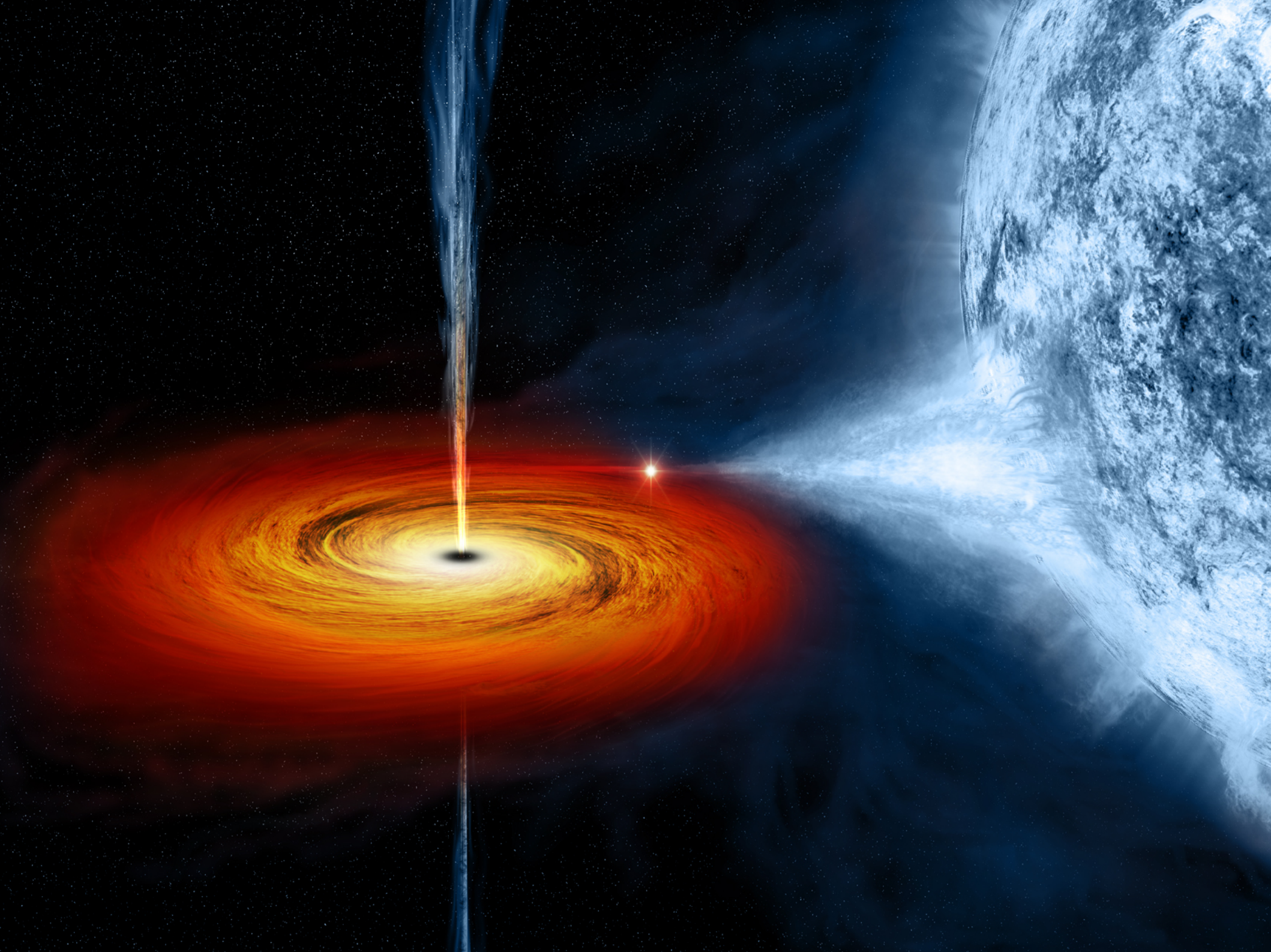
# Astrophysical black holes

The spacetime metric around astrophysical black holes formed from gravitational collapse should be **well approximated** by the Kerr solution:

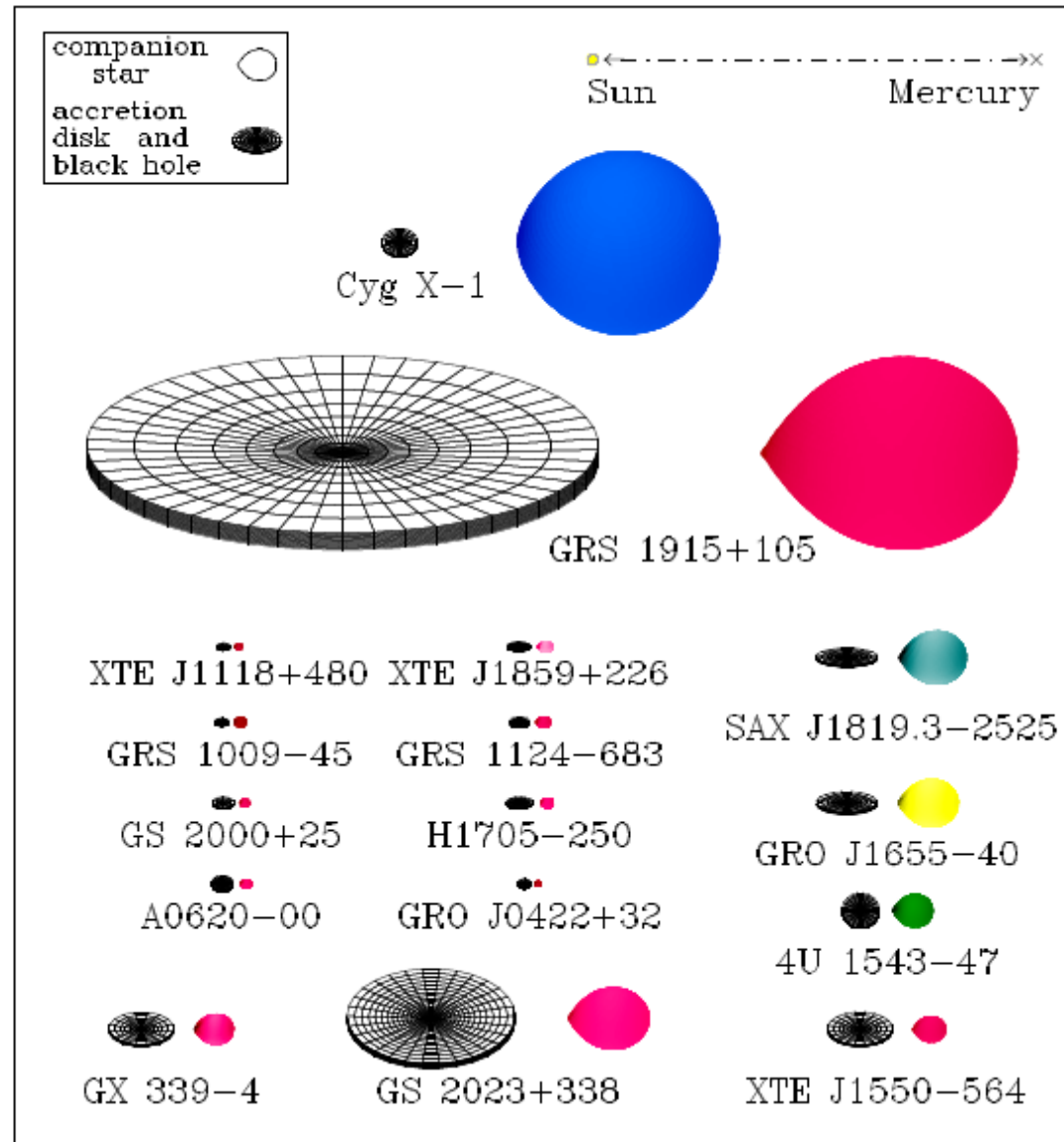
- Initial deviations are radiated away by gravitational waves
- Equilibrium electric charge is negligible
- Mass of the accretion disk is negligible

# Black hole “candidates”

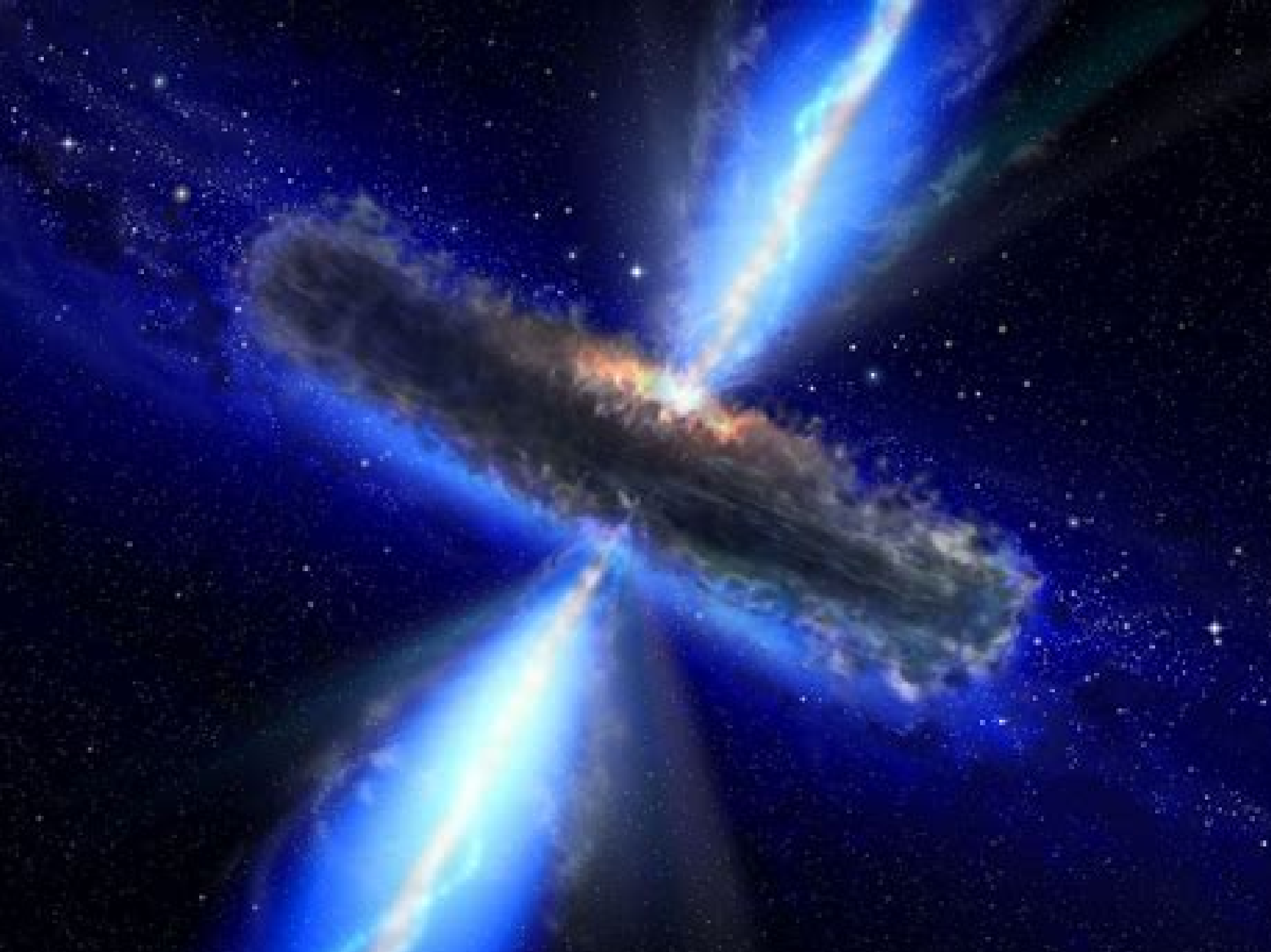
- **Stellar-mass black holes (3 – 100 Solar masses)**
- **Supermassive black holes ( $10^5 – 10^{10}$  Solar masses)**
- **Intermediate-mass black holes ( $10^2 – 10^4$  Solar masses?)**



# Black Hole Binaries in the Milky Way

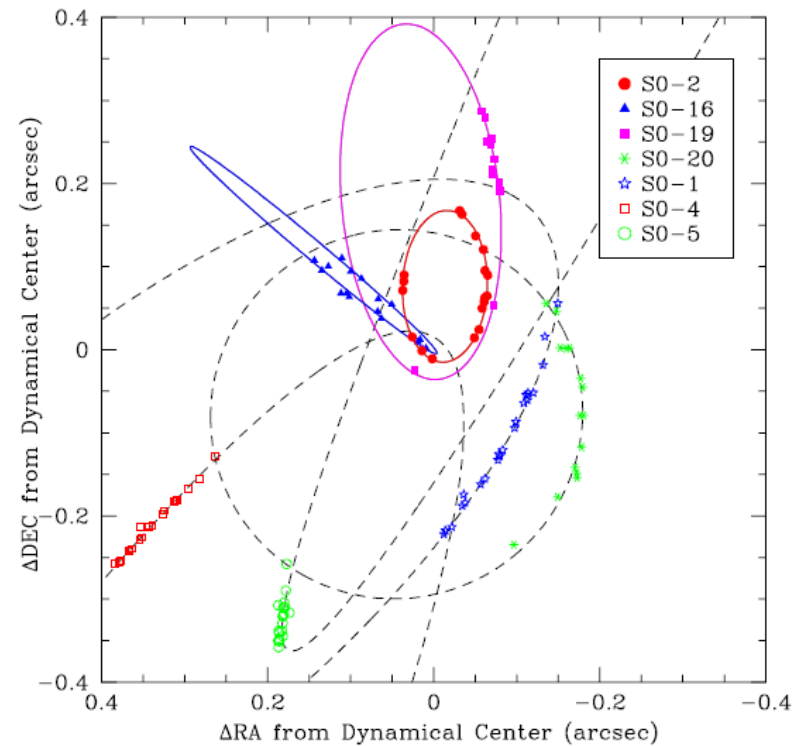


**Figure courtesy of Jerome Orosz**



# Supermassive BH candidate in the Galaxy

- **Orbital motion of individual stars**
- **Point-like central object with a mass of  $4 \times 10^6$  Solar masses**
- **Radius  $< 45$  AU ( $600 R_{\text{Sch}}$ )**



**From Ghez et al. 2005**

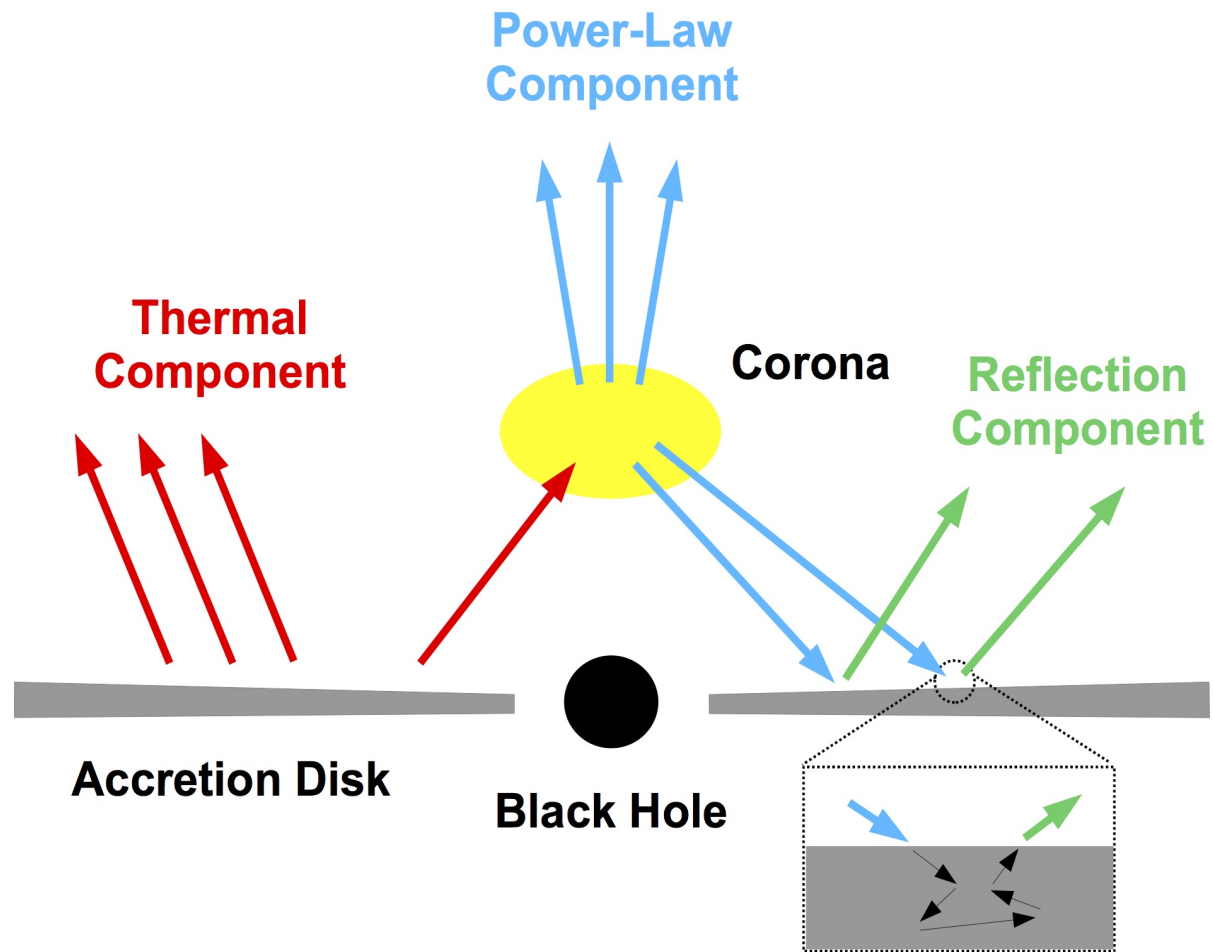


**Black holes “candidates” → Dark and compact objects that can be naturally interpreted as the Kerr black holes predicted in General Relativity**

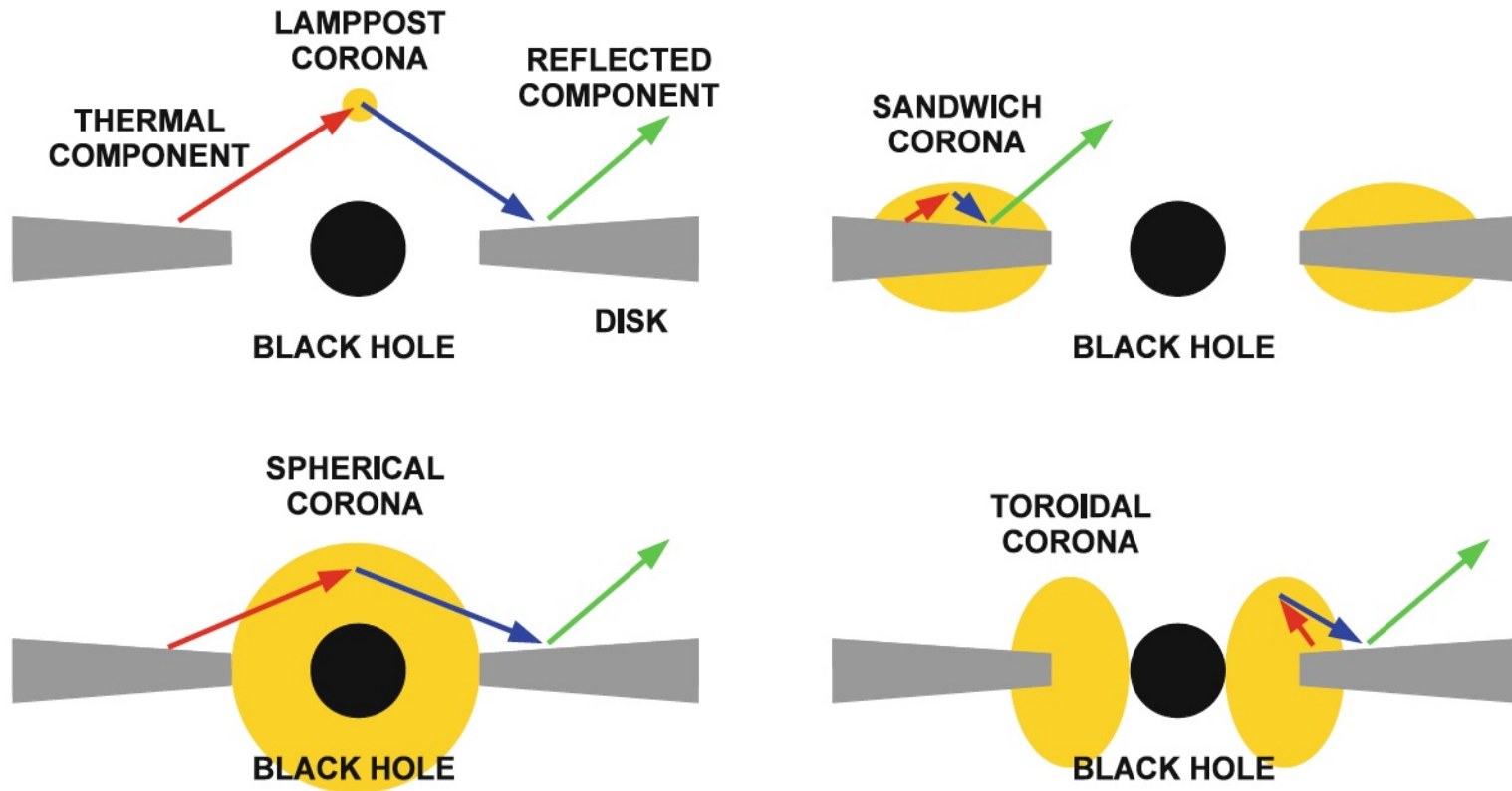
**We want to observationally test whether the spacetime metric is described by the Kerr solution**

# Method

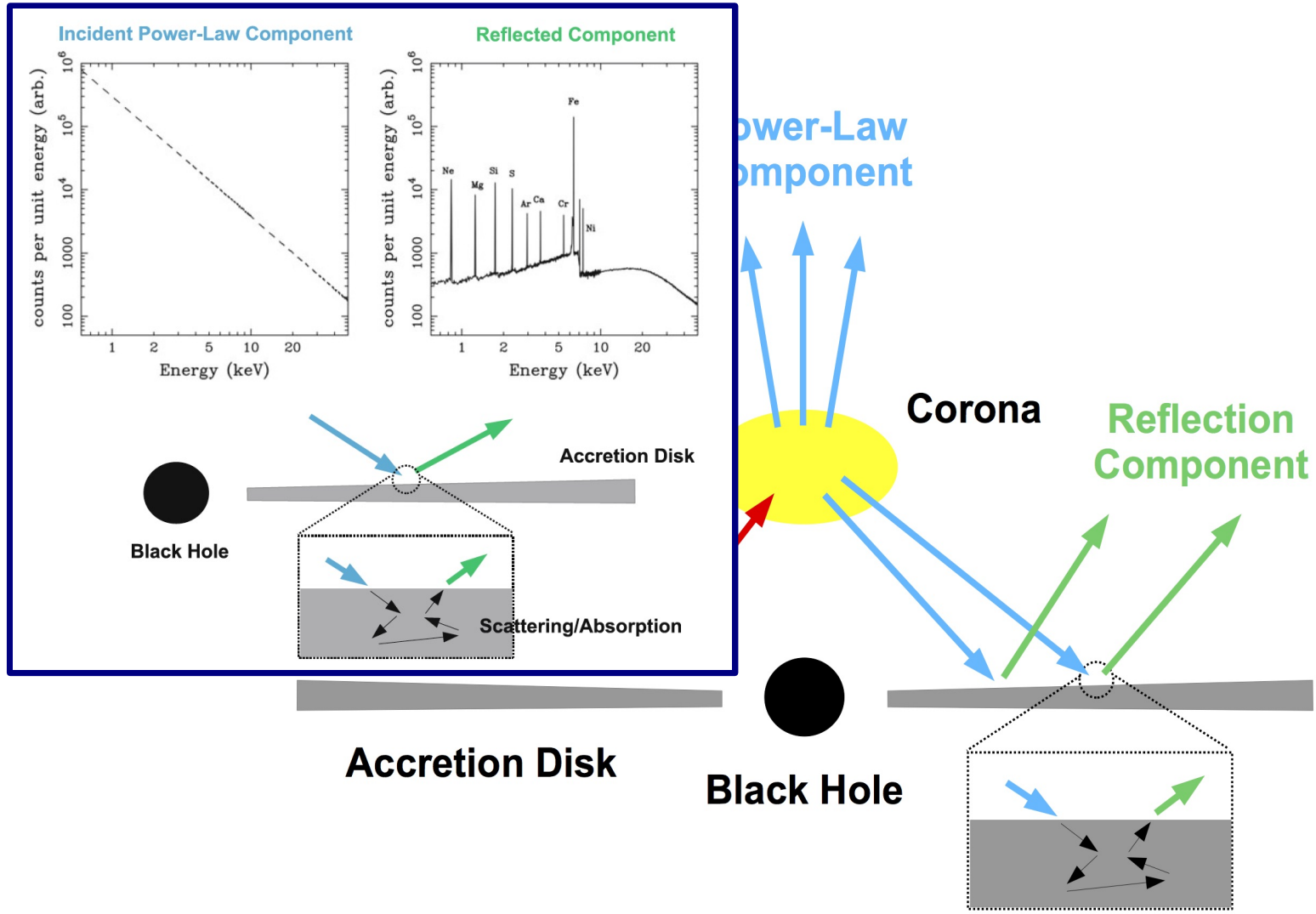
# Disk-corona model



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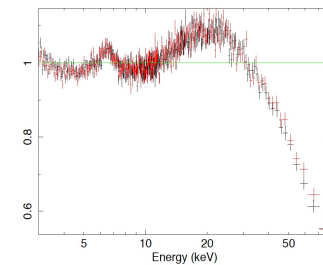
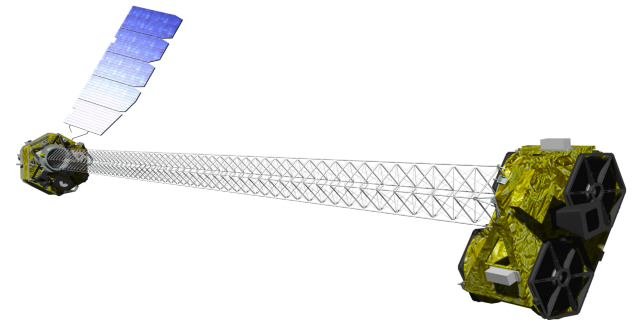
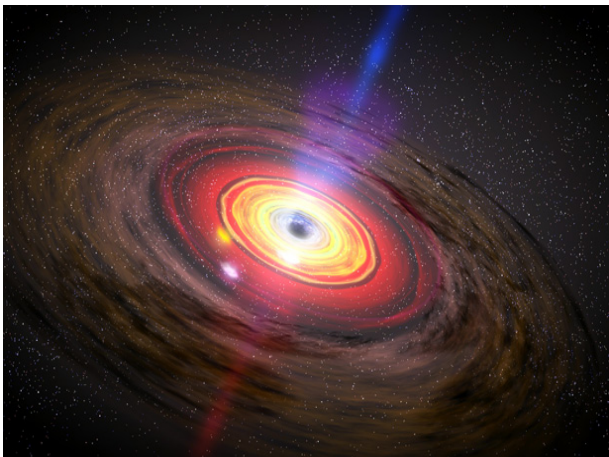


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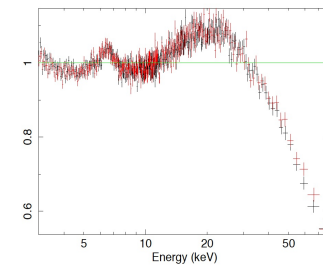
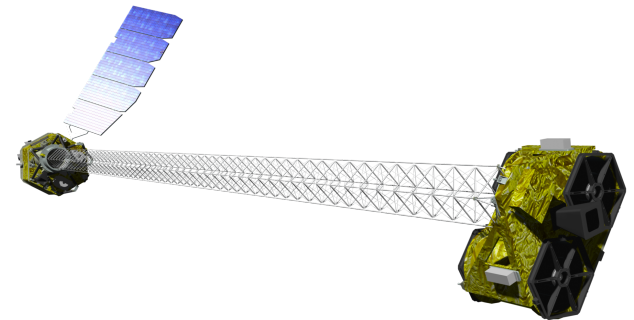
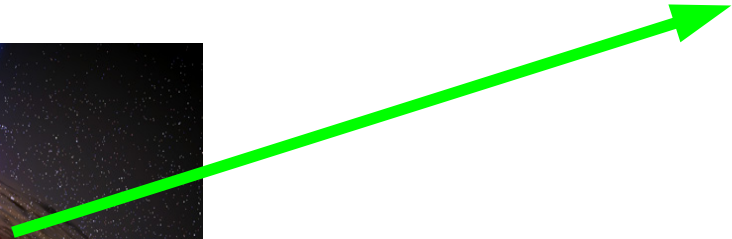
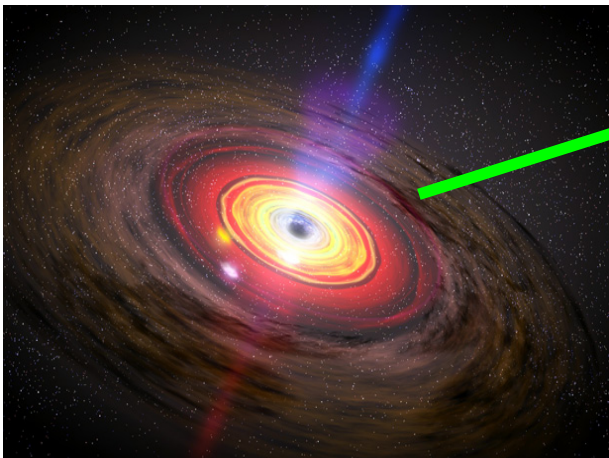
# Reflection spectrum

- Reflection spectrum at the emission point → Atomic physics
- Reflection spectrum far from the source → Einstein's gravity



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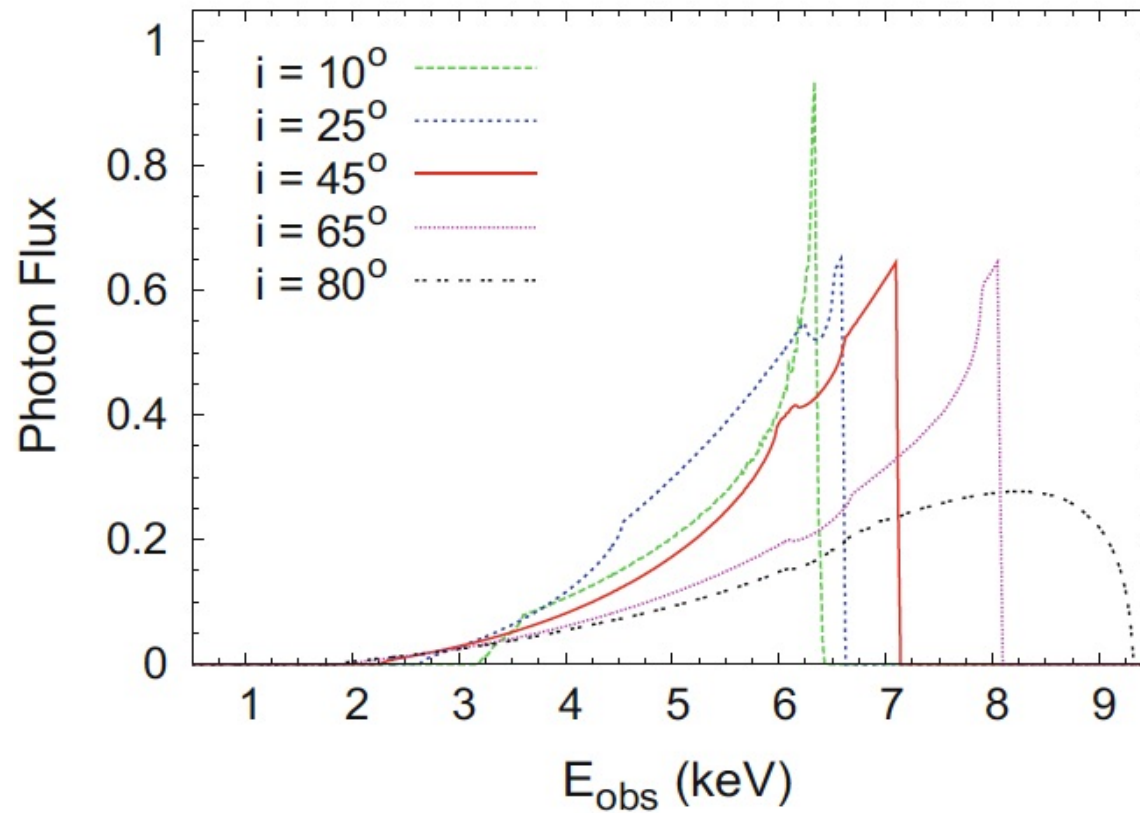
**Model**



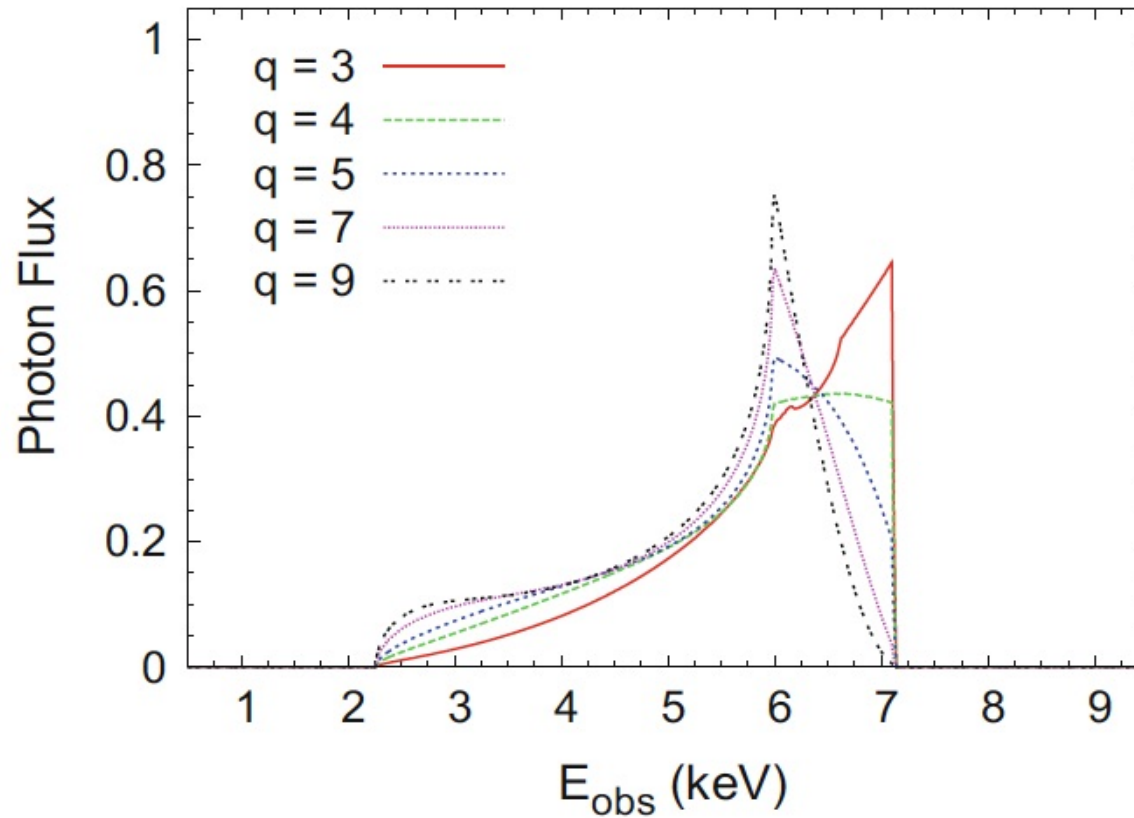
# RELXILL

- **RELXILL is currently the most advanced X-ray reflection model for Kerr spacetimes**
- **Reflection spectrum at the emission point → XILLVER**
- **Reflection spectrum far from the source (assuming Einstein's gravity)  
→ RELXILL ~ RELCOV\*XILLVER**
- **RELXILL can be employed to measure black hole spins**

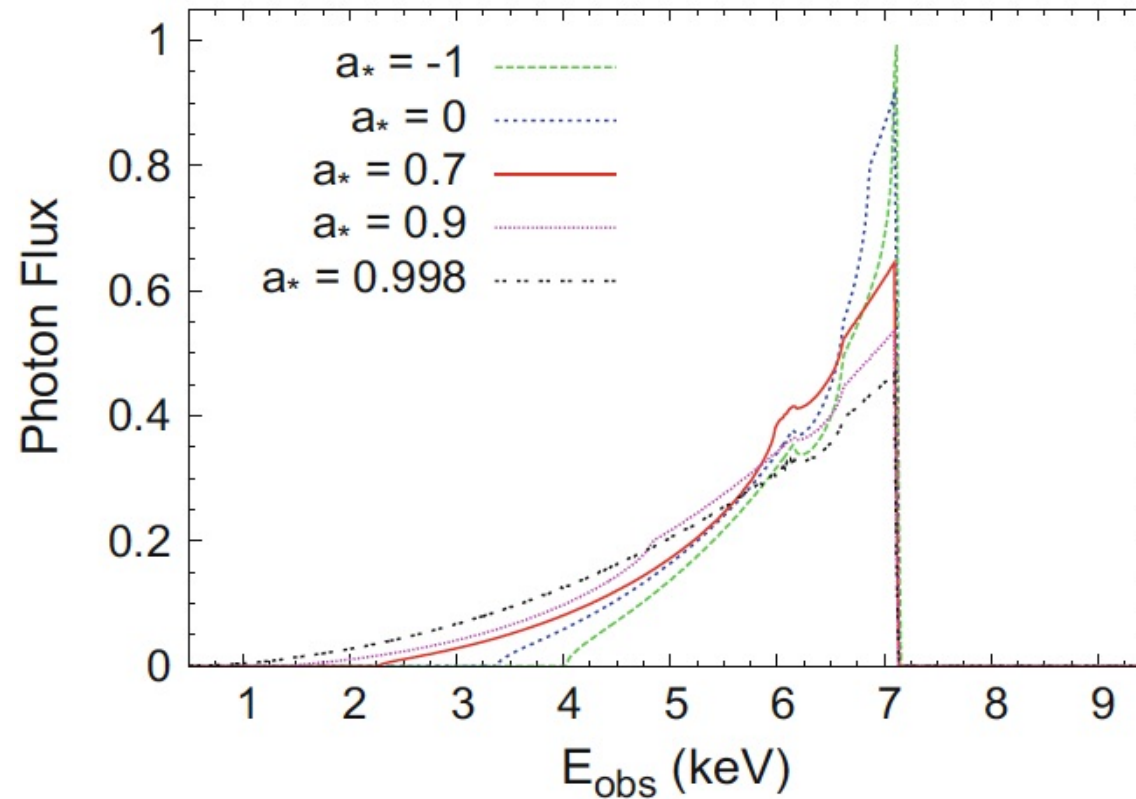
# Impact of the inclination angle



# Impact of the emissivity index



# Impact of the spin parameter



# Current spin measurements

BH Binary	$a_*$ (continuum)	$a_*$ (iron)	Principal References
GRS 1915-105	$> 0.98$	$0.98 \pm 0.01$	[21, 23]
Cyg X-1	$> 0.98$	$0.97^{+0.014}_{-0.02}$	[12, 13, 8, 25]
LMC X-1	$0.92 \pm 0.06$	$0.97^{+0.02}_{-0.25}$	[10, 36]
GX 339-4	$< 0.9$	$0.95 \pm 0.03$	[14, 27, 9]
MAXI J1836-194	—	$0.88 \pm 0.03$	[28]
M33 X-7	$0.84 \pm 0.05$	—	[18]
4U 1543-47	$0.80 \pm 0.10^*$	—	[31]
IC10 X-1	$\gtrsim 0.7$	—	[34]
Swift J1753.5	—	$0.76^{+0.11}_{-0.15}$	[26]
XTE J1650-500	—	$0.84 \sim 0.98$	[37]
GRO J1655-40	$0.70 \pm 0.10^*$	$> 0.9$	[31, 26]
GS 1124-683	$0.63^{+0.16}_{-0.19}$	—	[4, 24]
XTE J1752-223	—	$0.52 \pm 0.11$	[29]
XTE J1652-453	—	$< 0.5$	[5]
XTE J1550-564	$0.34 \pm 0.28$	$0.55^{+0.15}_{-0.22}$	[35]
LMC X-3	$0.25 \pm 0.15$	—	[32]
H1743-322	$0.2 \pm 0.3$	—	[33]
A0620-00	$0.12 \pm 0.19$	—	[11]
XMMU J004243.6	$< -0.2$	—	[22]

**Table 6.1** Summary of the continuum-fitting and iron line measurements of the spin parameter of stellar-mass black hole candidates under the assumption of the Kerr background. See the references in the last column for more details. \*These sources were studied in an early work of the continuum-fitting method, within a more simple model, and therefore here the published  $1\sigma$  error estimates are doubled.

# Current spin measurements

AGN	$a_*$ (iron)	$L_{\text{Bol}}/L_{\text{Edd}}$	Principal References
IRAS 13224-3809	$> 0.995$	0.71	[36]
Mrk 110	$> 0.99$	$0.16 \pm 0.04$	[36]
NGC 4051	$> 0.99$	0.03	[24]
MCG-6-30-15	$> 0.98$	$0.40 \pm 0.13$	[4, 22]
1H 0707-495	$> 0.98$	$\sim 1$	[26, 36, 39]
NGC 3783	$> 0.98$	$0.06 \pm 0.01$	[5, 24]
RBS 1124	$> 0.98$	0.15	[36]
NGC 1365	$0.97^{+0.01}_{-0.04}$	$0.06^{+0.06}_{-0.04}$	[29, 30, 6]
Swift J0501.9-3239	$> 0.96$	—	[36]
Ark 564	$0.96^{+0.01}_{-0.06}$	$> 0.11$	[36]
3C 120	$> 0.95$	$0.31 \pm 0.20$	[18]
Ark 120	$0.94 \pm 0.01$	$0.04 \pm 0.01$	[25, 23, 36]
Ton S180	$0.91^{+0.02}_{-0.09}$	$2.1^{+3.2}_{-1.6}$	[36]
1H 0419-577	$> 0.88$	$1.3 \pm 0.4$	[36]
Mrk 509	$0.86^{+0.02}_{-0.01}$	—	[36]
IRAS 00521-7054	$> 0.84$	—	[33]
3C 382	$0.75^{+0.07}_{-0.04}$	—	[36]
Mrk 335	$0.70^{+0.12}_{-0.01}$	$0.25 \pm 0.07$	[25, 36]
Mrk 79	$0.7 \pm 0.1$	$0.05 \pm 0.01$	[9, 10]
Mrk 359	$0.7^{+0.3}_{-0.5}$	0.25	[36]
NGC 7469	$0.69 \pm 0.09$	—	[25]
Swift J2127.4+5654	$0.6 \pm 0.2$	$0.18 \pm 0.03$	[21, 25]
Mrk 1018	$0.6^{+0.4}_{-0.7}$	0.01	[36]
Mrk 841	$> 0.56$	0.44	[36]
Fairall 9	$0.52^{+0.19}_{-0.15}$	$0.05 \pm 0.01$	[25, 17, 31, 36]

**Table 7.1** Summary of the iron line measurements of the spin parameter of supermassive black hole candidates under the assumption of the Kerr background. See the references in the last column and [3] for more details.

# RELXILL\_NK

- **RELXILL\_NK is the natural extension of RELXILL for non-Kerr spacetimes**
  - **RELXILL\_NK ~ RELCOV\_NK\*XILLVER**
- **“Deformation parameters”**
- **RELXILL\_NK can be employed to test the Kerr black hole hypothesis**

# How can we test the Kerr nature of astrophysical black holes?

- **Top-down approach:**

**We test a specific alternative theory of gravity against Einstein's gravity**

**Problems:**

**1) A large number of alternative theories...**

**2) We do not have rotating black hole solutions...**

- **Bottom-up approach:**

**See PPN formalism**



# Solar System experiments: Schwarzschild solution in the weak field limit

- **Parametrized Post-Newtonian formalism (PPN formalism)**
- **Weak field limit ( $M/r \ll 1$ )**
- **Solar System experiments**

$$ds^2 = - \left( 1 - \frac{2M}{r} + \beta \frac{2M^2}{r^2} + \dots \right) dt^2 + \left( 1 + \gamma \frac{2M}{r} + \dots \right) (dx^2 + dy^2 + dz^2)$$

$$|\beta - 1| < 2.3 \cdot 10^{-4} \quad (\text{Lunar Laser Ranging experiment})$$

$$|\gamma - 1| < 2.3 \cdot 10^{-5} \quad (\text{Cassini spacecraft})$$

In general relativity  $\beta = \gamma = 1$

# Johannsen metric

**[Johannsen, PRD 88, 044002 (2013)]**

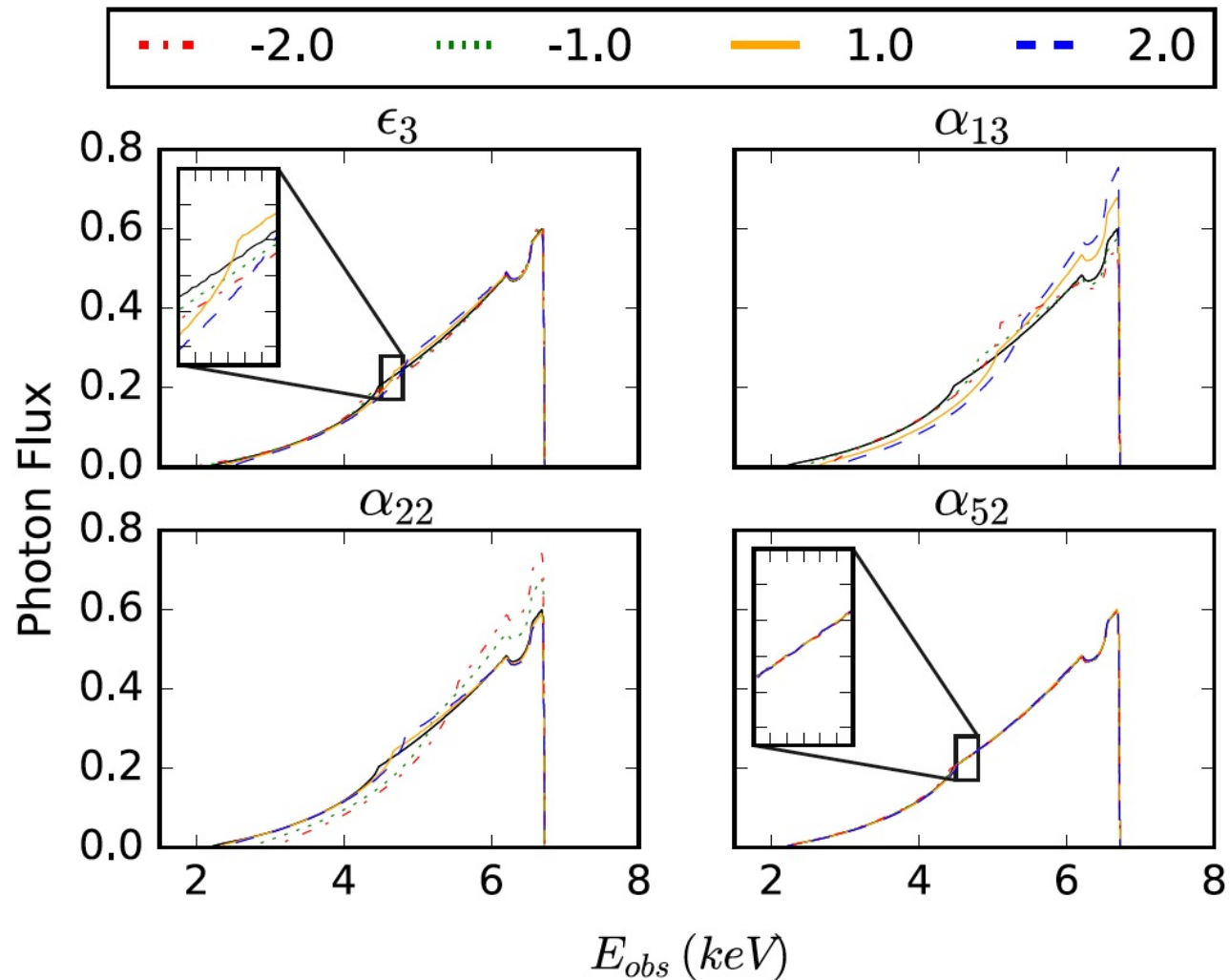
$$\begin{aligned}
 ds^2 = & -\frac{\tilde{\Sigma}(\Delta - a^2 A_2^2 \sin^2 \theta)}{B^2} dt^2 \\
 & -\frac{2a[(r^2 + a^2)A_1 A_2 - \Delta]\tilde{\Sigma} \sin^2 \theta}{B^2} \\
 & \times dt d\phi + \frac{\tilde{\Sigma}}{\Delta A_5} dr^2 + \tilde{\Sigma} d\theta^2 \\
 & + \frac{[(r^2 + a^2)^2 A_1^2 - a^2 \Delta \sin^2 \theta]\tilde{\Sigma} \sin^2 \theta}{B^2} d\phi^2,
 \end{aligned}$$

$$\begin{aligned}
 B &= (r^2 + a^2)A_1 - a^2 A_2 \sin^2 \theta, & \tilde{\Sigma} &= \Sigma + f, \\
 \Sigma &= r^2 + a^2 \cos^2 \theta, & \Delta &= r^2 - 2Mr + a^2,
 \end{aligned}$$

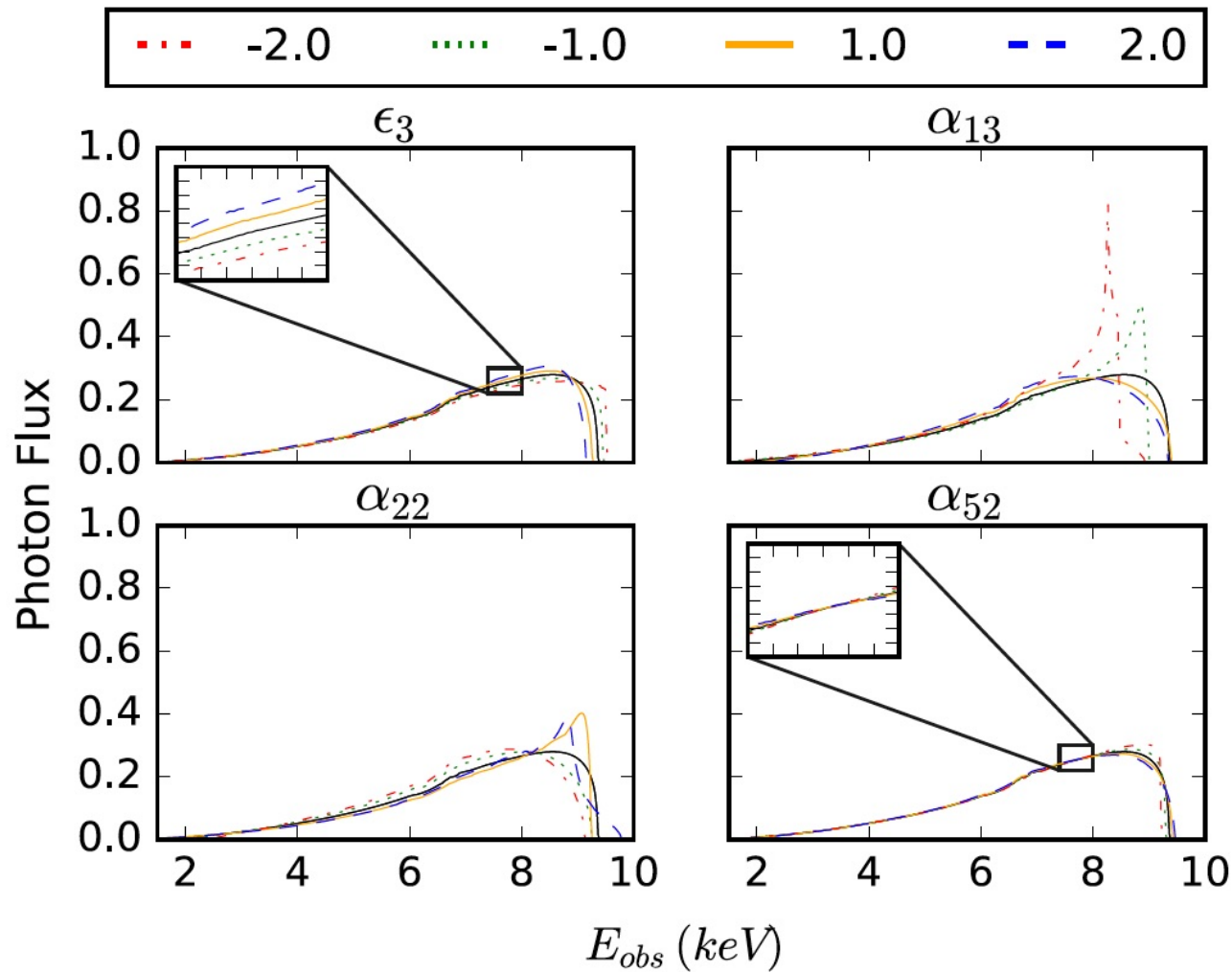
$$f = \epsilon_3 \frac{M^3}{r}, \quad A_1 = 1 + \alpha_{13} \left(\frac{M}{r}\right)^3,$$

$$A_2 = 1 + \alpha_{22} \left(\frac{M}{r}\right)^2, \quad A_5 = 1 + \alpha_{52} \left(\frac{M}{r}\right)^2.$$

# Impact of the deformation parameters ( $i = 30$ deg)



# Impact of the deformation parameters ( $i = 80$ deg)

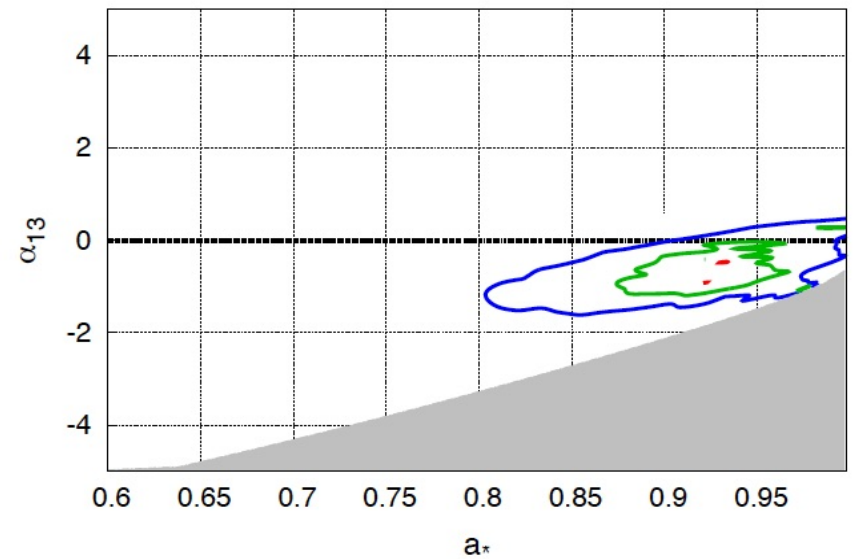
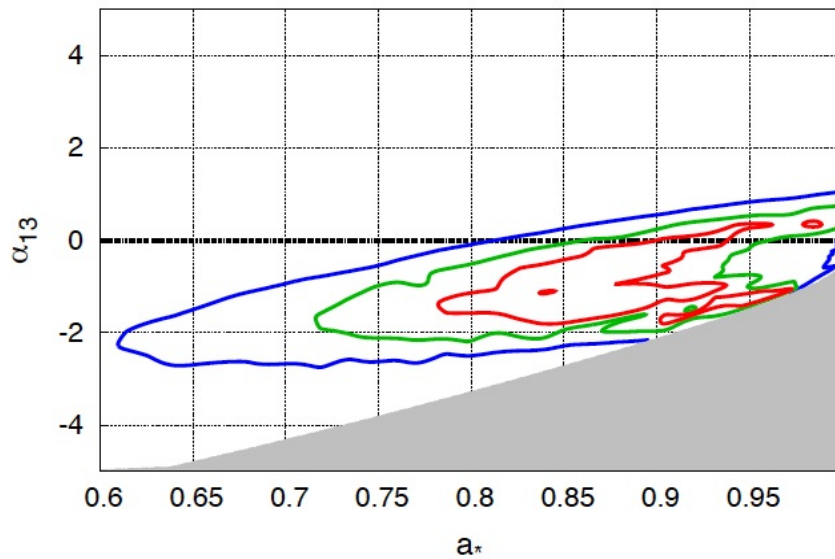


# Results

# Sources

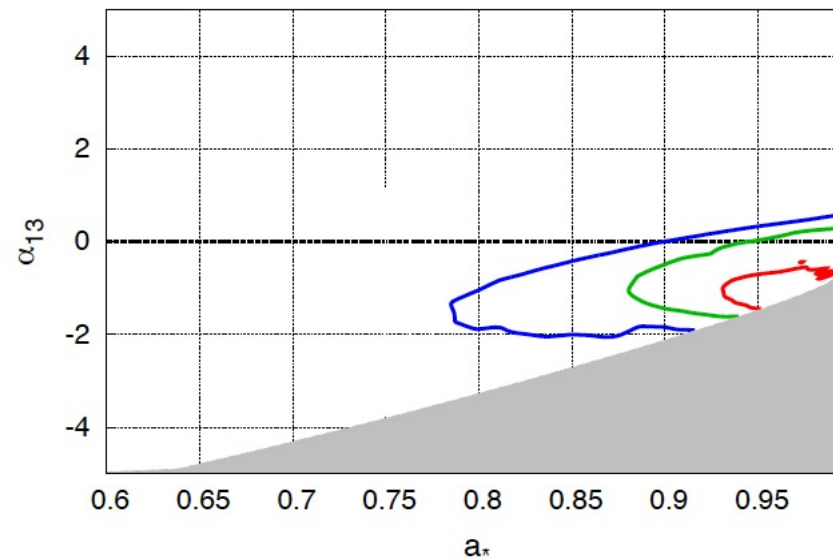
- **1H0707-495 (Cao et al., PRL 120, 051101, 2018; Zhou et al. PRD 024007, 2018)**
- **Ark 564 with Suzaku data (Tripathi et al., PRD 98, 023018, 2018)**
- **GX339-4 with RXTE data (Wang-Ji et al., arXiv:1806.00126)**
- **GS 1354-645 with NuSTAR (Xu et al., ApJ, 865, 134, 2018)**
- **Mrk 335 with Suzaku (Choudhury et al., arXiv:1809.06669)**
  
- **Cygnus X-1 with NuSTAR data (in preparation)**
- **MCG-6-30-15 with XMM-Newton+NuSTAR (in preparation)**
- ...

# 1H0707-495: XMM-Newton data of 2011



**Cao et al., PRL 120, 051101 (2018)**

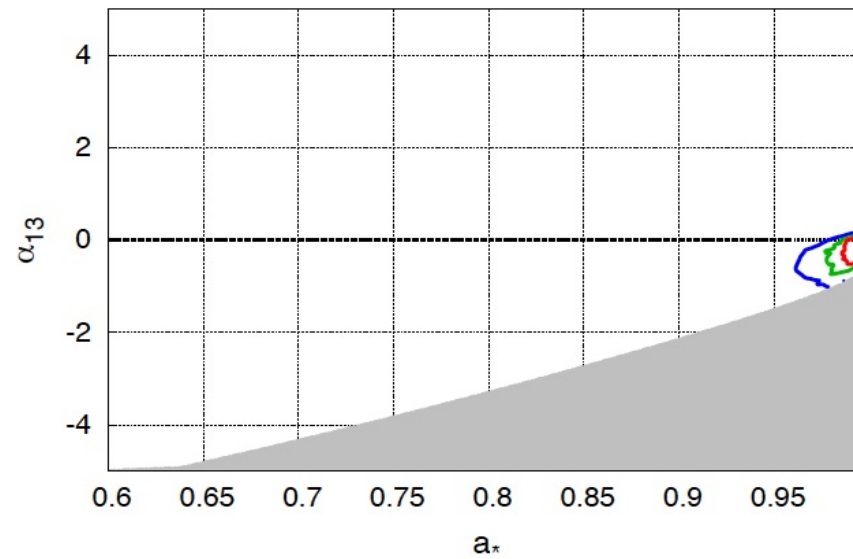
# 1H0707-495: NuSTAR+Swift



**Cao et al., PRL 120, 051101 (2018)**

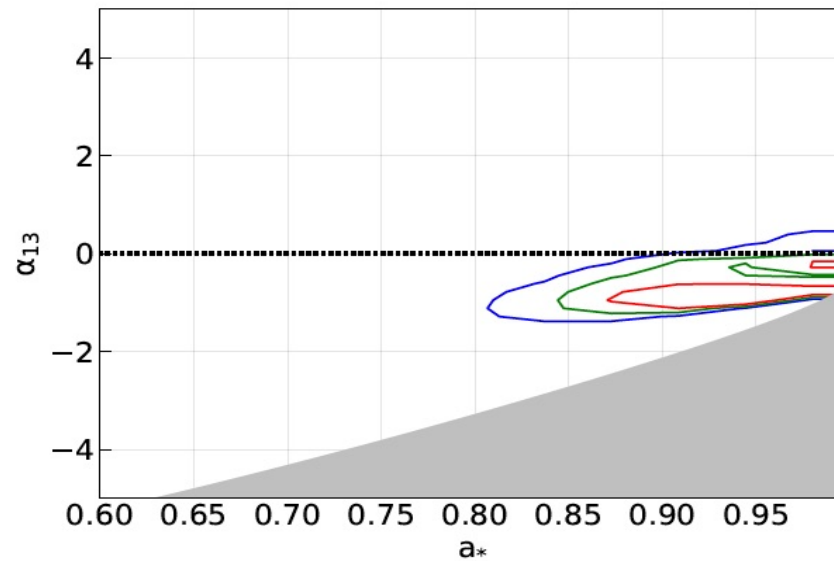


# Ark 564: Suzaku



**Tripathi et al., PRD 98, 023018 (2018)**

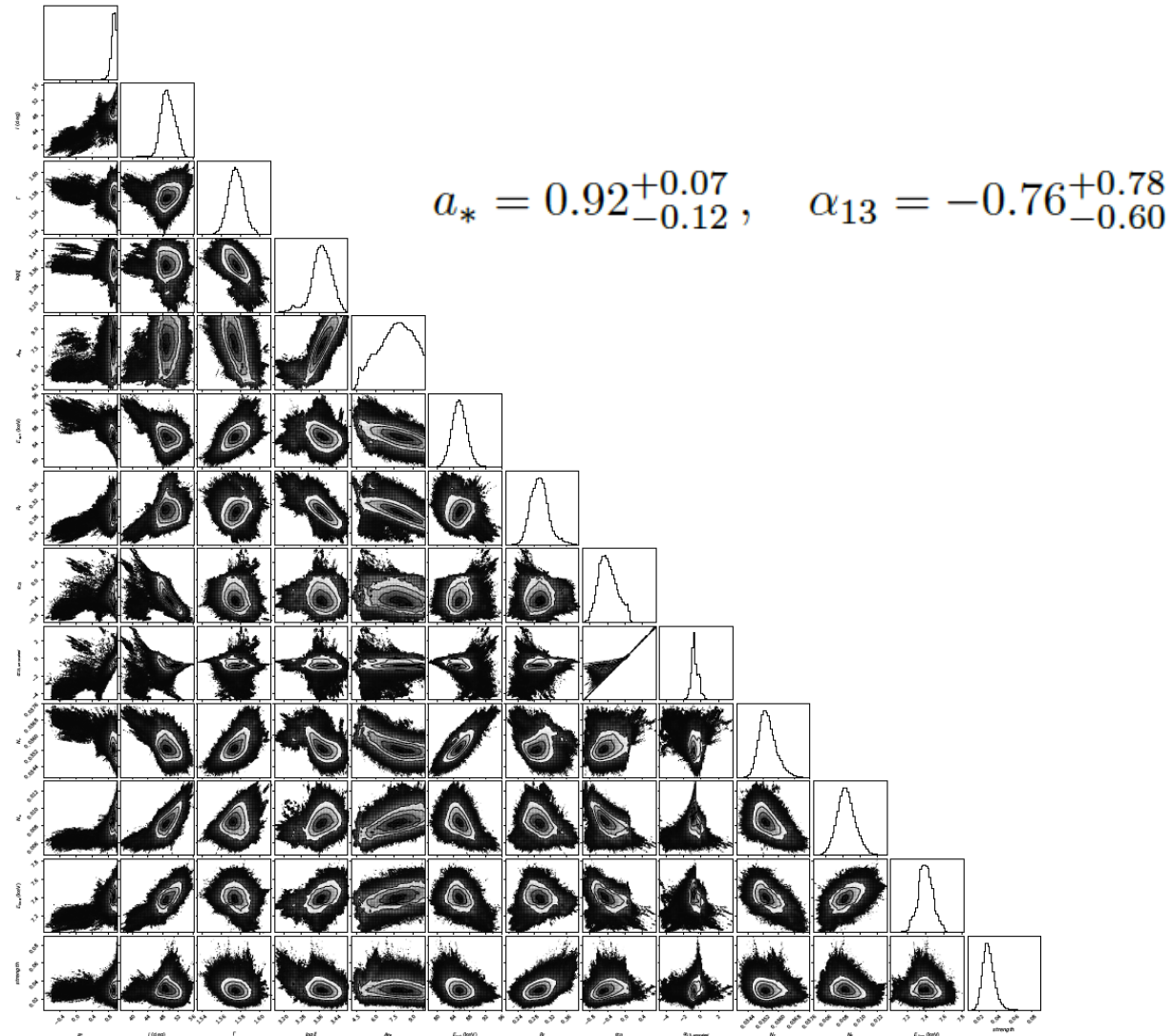
# GX 339-4: RXTE



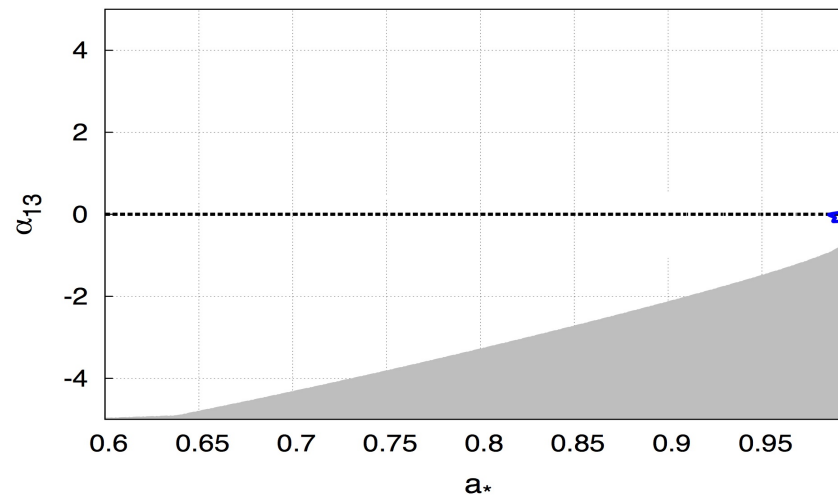
**Wang-Ji et al., arXiv:1806.00126**

# GX 339-4: RXTE

Wang-Ji et al., arXiv:1806.00126



# GS 1354: NuSTAR



**Xu et al., ApJ 865, 134 (2018)**

# **Conclusions**

# Road map

**Last 3 years (2016-2018):**

- **Astrophysical model (RELXILL\_NK, Bambi et al. ApJ 842, 76, 2017)**
- **Preliminary observational constraints (Cao et al. PRL 120, 051101, 2018 etc. + papers under review or in preparation)**

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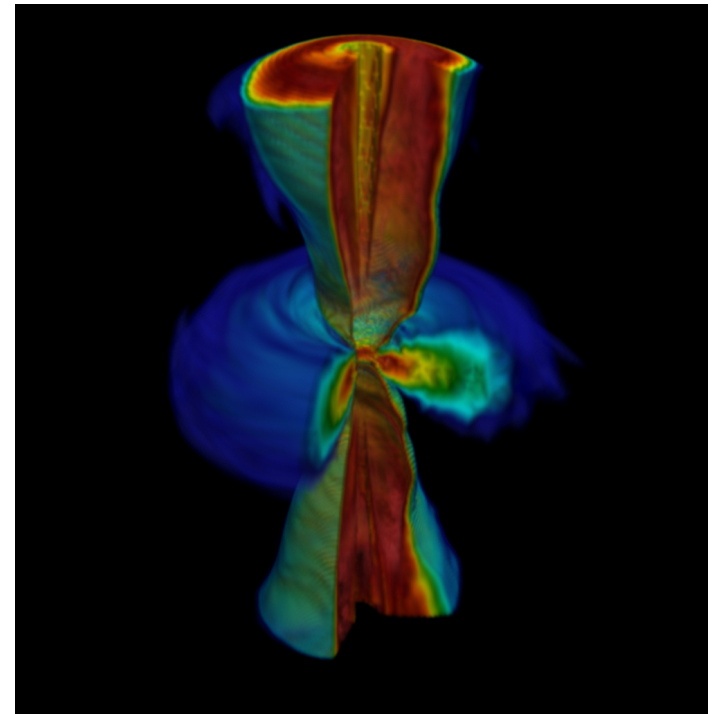
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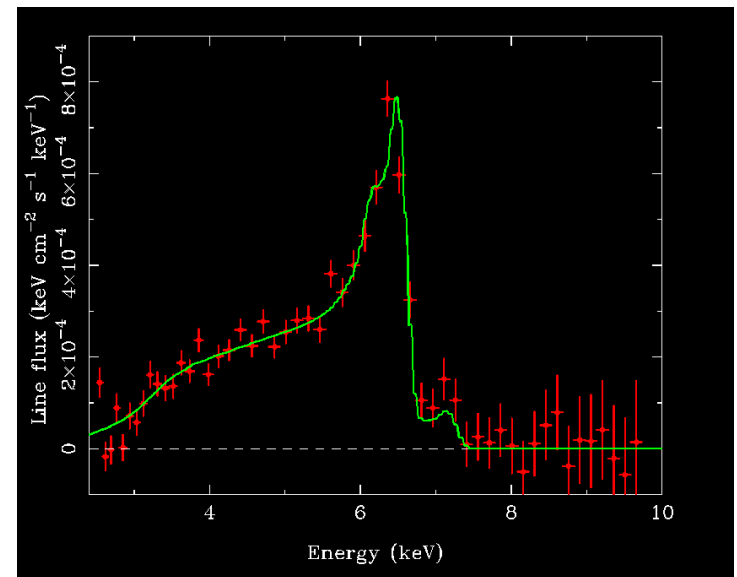
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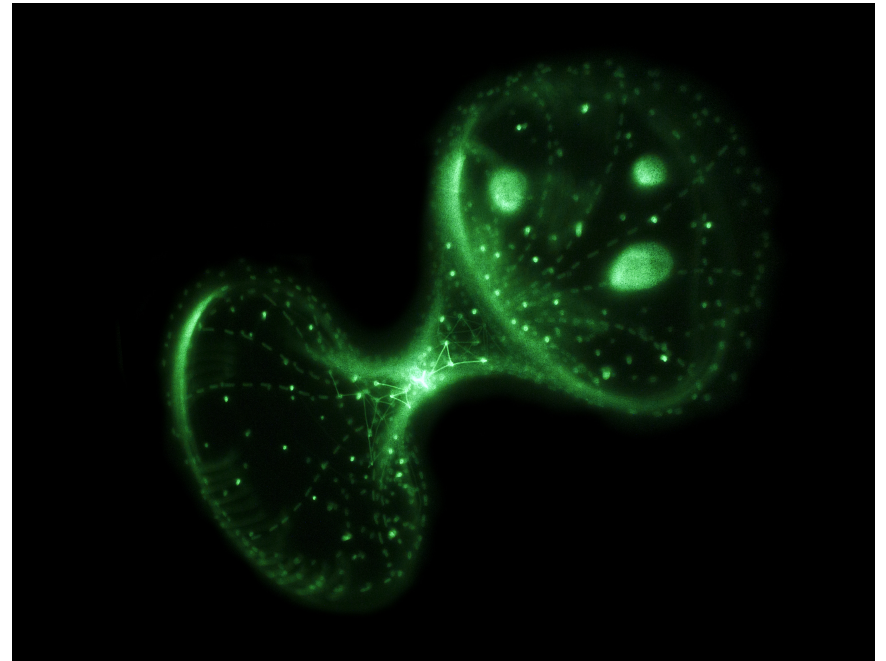
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**Thank you!**

# PhD positions at Fudan University

- **Fudan University (Shanghai, China)**

**3<sup>rd</sup> in China, 44<sup>th</sup> in the world (QS World University Ranking 2019)**

- **International PhD students**

**Application deadline: November 30**

**Requirements: Master degree before September 2019**

**Application procedure: CV, at least 2 recommendation letters**

**[bambi@fudan.edu.cn](mailto:bambi@fudan.edu.cn)**

**<https://hyperspace.uni-frankfurt.de/2018/10/01/phd-positions-in-astrophysics-gravity-at-fudan-university-shanghai-china/>**